

## Pascal and gambling logic

# Early decision theory & **utility maximization**

Understanding the  
logic of gambling  
decisions



Blaise Pascal, Mathematician

<https://en.wikipedia.org/>

# decisions, decisions...



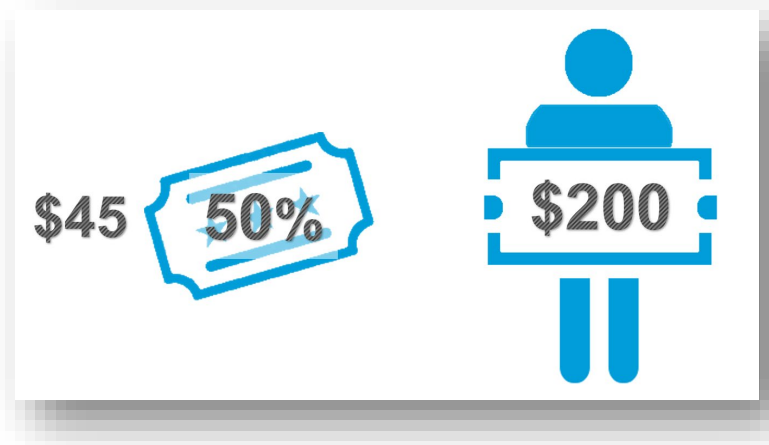
Lottery ticket costs \$45.  
It has a 50% chance of winning \$200



buy  
ticket



Blaise Pascal, Mathematician



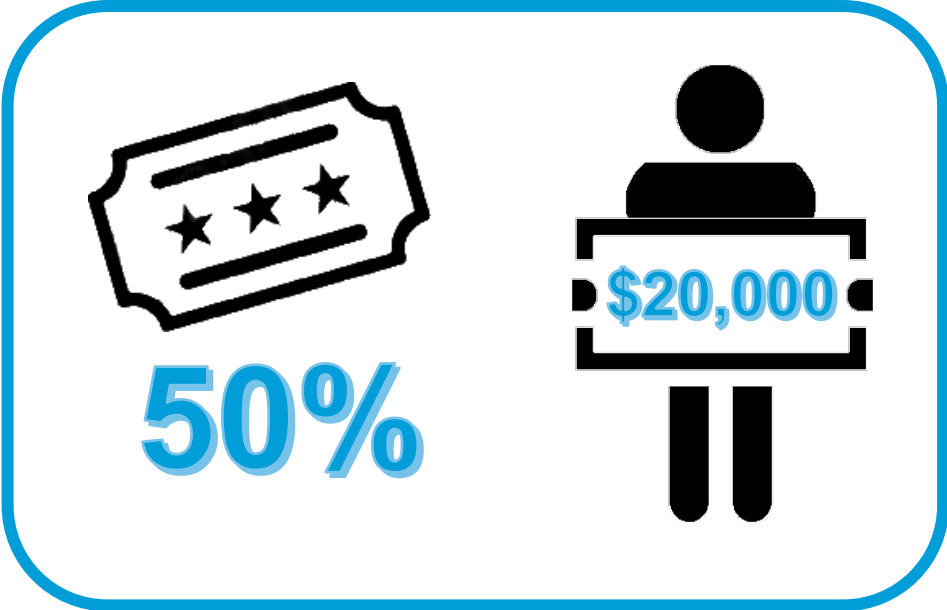
Expected value = the probability of winning X the amount to be won

$$EV = 0.5 \times 200 = 100$$

ticket  
price

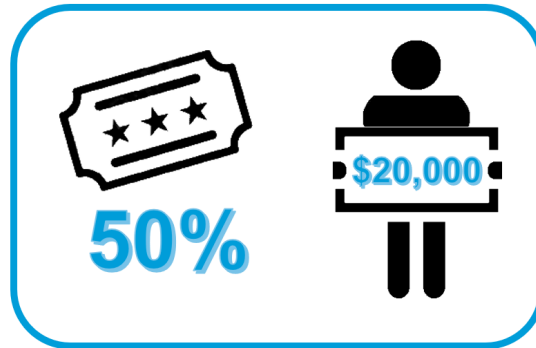
→  $\$45 < \$100$

# Consider a **poor** person...





I'll give you  
**\$7,000** for  
the ticket.



**Daniel Bernoulli:**



one should maximize  
expected **utility**

**He makes a distinction between:  
expected value and expected utility.**

# Prospect Theory

people *evaluate potential changes*  
in

**relative wealth,**  
**not absolute wealth**



Famous Kahneman and Tversky experiment:



**Start  
with  
\$1000**

Choose  
between:

50/50 chance of  
winning \$1000 or \$0

Get \$500



**Start  
with  
\$2000**

Choose  
between:

50/50 chance of  
losing 1000 or 0

Lose \$500



**Framing matters.**

# A reverse sunk cost effect in risky decision making: Sometimes we have too much invested to gamble <sup>1</sup>

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Received 5 January 1996; accepted 27 April 1997

## Abstract

The sunk cost effect refers to the empirical finding that people tend to let their decisions be influenced by costs made at an earlier time in such a way that they are more risk seeking than they would be had they not made these costs. This finding seems to be in conflict with economic theory which implies that only incremental costs and benefits should affect decisions. The effect is often explained in terms of prospect theory of (Kahneman, D., Tversky, A., 1979. Prospect theory: An analysis of decision under risk. *Econometrica* 47, 263–291), suggesting that sunk costs may induce a ‘loss frame,’ consequently causing risk seeking behavior. We argue that sunk costs may also result in risk aversion. In the present study we investigated the effect of time and effort investments (Behavioral Sunk Costs) on risky decision making in gain and loss situations. The results show that, in agreement with prospect theory, participants were more risk averse in gain situations than in loss situations. Moreover, incurring Behavioral Sunk Costs appeared to increase risk aversive choices, i.e., a reverse sunk cost effect.

Costs made earlier in time

↑ risk seeking

Loss frame

→ risk behavior

# Fear of losing >



TREND HUNTER  
FUTURE  
FESTIVAL

1 DAY  
LEFT



SAVE  
UP TO  
96%

JANUARY  
SALE

LAST  
CHANCE

SHOP NOW >



START  
PANICKING  
ONLY  
5 TICKETS  
LEFT



DON'T  
MISS OUT!



FINAL  
HOURS!

20% OFF  
SITEWIDE

CODE: ASTRO

SHOP NOW



ENDING SOON!

BLACK  
FRIDAY

20% OFF sitewide.  
Use code: BLKFRIDAY



- Prospect Theory says that people evaluate potential changes in RELATIVE wealth, not in absolute wealth states.

- This is the most central idea in behavioral economics
- It will exert its influence in many key decisions.

# reference dependence

When faced with a risky decision we think less about our bank account and more about whether we will be better or worse off afterward.

# Loss Aversion and Endowment Effect



Dan Ariely



<https://www.youtube.com/watch?v=YpiGVWO-C64>



## Everyday example of reference points

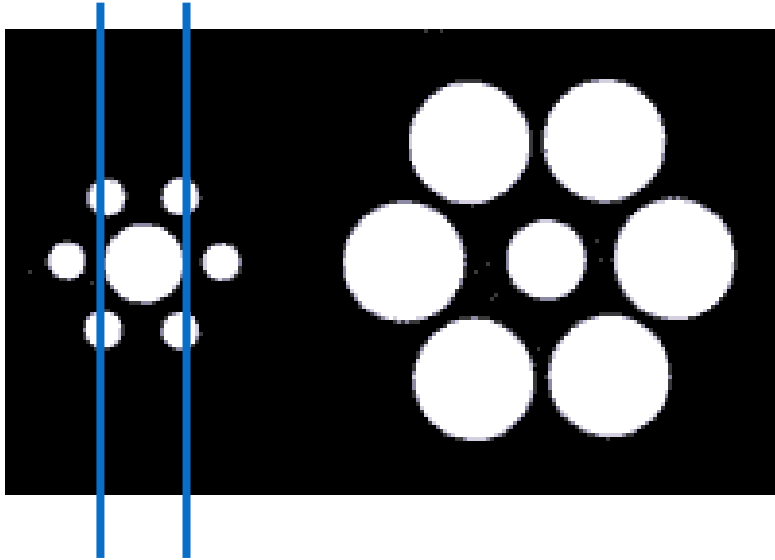


- ❑ Consumer's **love** sales!
- ❑ Marketers **love** sales because it is a reference point to the regular price
- ❑ *Not* saving money when buying something at 20% off.
- ❑ However, if one adopts the reference point of the merchandise as the regular price then the sale of 20% can seem psychologically like savings.

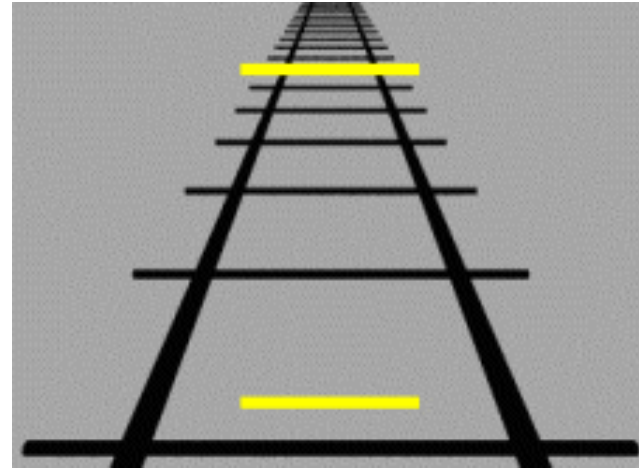




Is the left center circle larger?

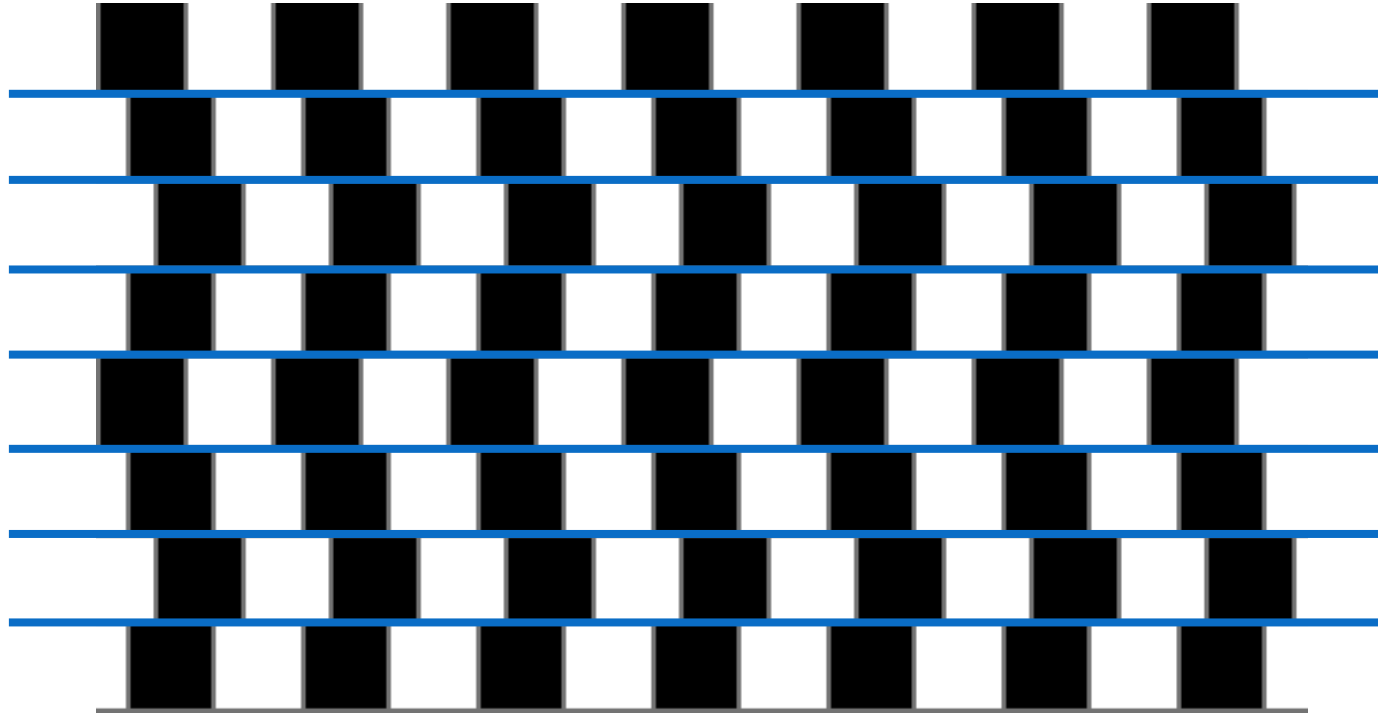


Is the top yellow line longer?





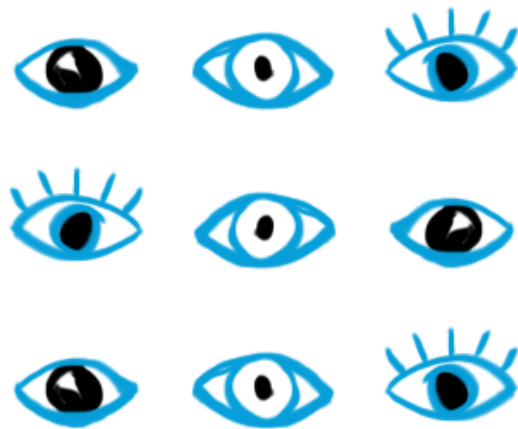
Are these lines straight or crooked?





How do you represent something with **sufficient range** to accommodate **big numbers** and **sufficient precision** to resolve differences between *small numbers*?

**visual system solves this**



**Range representation problem**



**10,000,000:1**

Humans can see over a light intensity range of several million to one.



## Surface luminance levels

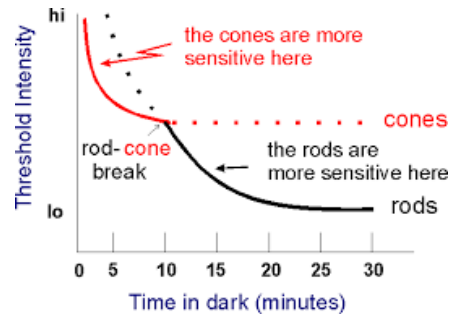
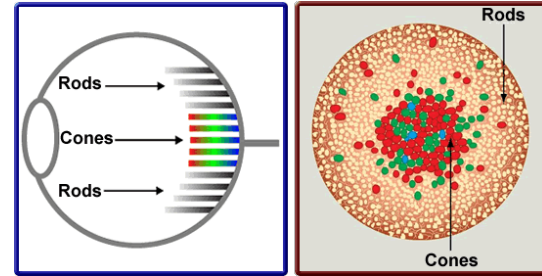
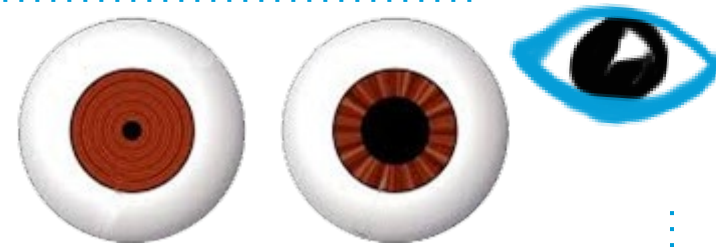
- Sunlight:  $10^5$  candelas/meter<sup>2</sup> ( $\text{cd}/\text{m}^2$ )
  - Approx.  $10^{22}$  photons/ $\text{m}^2/\text{sec}$
  - 3%-90% of photons are reflected as luminance
  - 3% for black surfaces, 90% for white surfaces
  - Only some of the reflected photons enter the pupil of eye
- Indoor lighting, CRTs:  $10^2$   $\text{cd}/\text{m}^2$
- Moonlight:  $10^{-1}$   $\text{cd}/\text{m}^2$
- Starlight:  $10^{-3}$   $\text{cd}/\text{m}^2$
- The eye can adjust to changes in light level by a factor of 100,000,000!
- Yet firing rates only typically range from 0-400Hz.

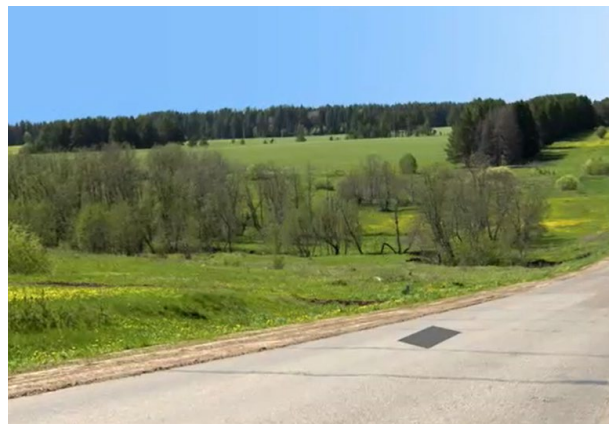
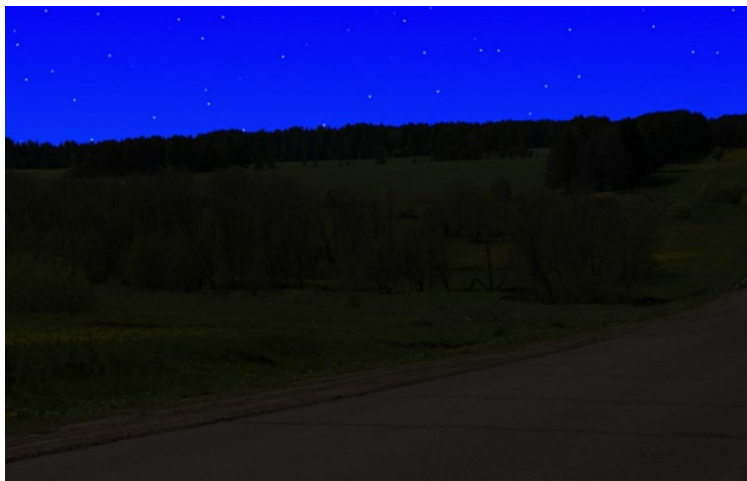
[www.cns.nyu.edu/~david/courses/perception/lecturenotes/light-adapt/light-adapt.html](http://www.cns.nyu.edu/~david/courses/perception/lecturenotes/light-adapt/light-adapt.html)

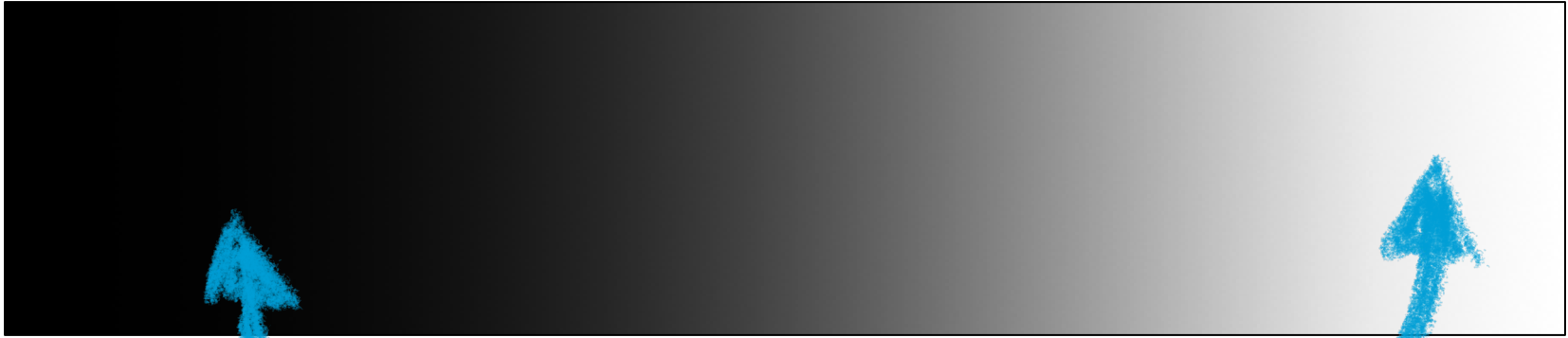
## Mechanisms of light/dark adaptation

1. Pupil size
2. Switchover between rods and cones
3. Bleaching/regeneration of photopigment
4. Feedback from horizontal cells to control the responsiveness of photoreceptors

[www.cns.nyu.edu/~david/courses/perception/lecturenotes/light-adapt/light-adapt.html](http://www.cns.nyu.edu/~david/courses/perception/lecturenotes/light-adapt/light-adapt.html)







At night, tiny changes in absolute brightness change the neurons firing rate

During the day, in bright light, the reference point increases and greater changes in absolute brightness are required to alter the firing rate of a neuron.